

# Luis Modes

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“Being happy is the greatest form of success.” – unknown

## Research Interests

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Algebraic geometry, arithmetic geometry, and topology

## Profile

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**Languages:** English (fluent), Spanish (native), and Japanese (intermediate)

**Programming:** Python, L<sup>A</sup>T<sub>E</sub>X, and SageMath

**Skills:** Problem-solving, math olympiad coaching, and mentoring

## Education

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Massachusetts Institute of Technology

*Undergraduate*

Cambridge, MA

*September 2021 – Present*

Academia Interamericana de Panamá sede Cerro Viento

*High School Diploma*

Panama, Panama

*March 2008 – December 2020*

## Selected Honors and Awards

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**Hartley Rogers Jr. Prize** for the best project of the MIT Math Department’s

Summer Program in Undergraduate Research (SPUR)

August 2024

**International Mathematical Olympiad (IMO):** Bronze Medal

July 2021

**International Mathematical Olympiad (IMO):** Bronze Medal

September 2020

**Panamanian Mathematical Olympiad:** Gold Medal, rank 1st in 2019 and 2020

2016 – 2020

**Asian Pacific Mathematical Olympiad (APMO):** Silver Medal

2019

## Research Experience

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**Summer Program in Undergraduate Research (SPUR)**

MIT 2024 - Present

- Generalized a theorem that identifies the spherical Hall algebra of  $\overline{\text{Spec}(\mathbb{Z})}$  with a shuffle algebra to a theorem about the spherical Hall algebra of  $\overline{\text{Spec}(\mathcal{O}_K)}$ , where  $K$  is a number field with class number 1 and  $\mathcal{O}_K$  is its ring of integers. Currently working on generalizing this theorem to any number field  $K$  through the Undergraduate Research Opportunities Program (UROP). Our paper can be found here: arXiv:2411.17055: The spherical Hall algebra of  $\overline{\text{Spec}(\mathcal{O}_K)}$ .

Reference: Zhiwei Yun

**18.821 Project Laboratory in Mathematics**

MIT 2024

- Worked with a group on two guided research problems. Wrote a paper and gave a presentation for each of them. The first problem was about exploring the density of integer solutions to the diophantine equation  $x^3 + y^3 = z^3 + w^3$ . The second problem was about exploring the density and existence of *happy sequences*: sequences of zeroes and ones invariant under replacing 0 with 10 and 1 with 100.

Reference: Roman Bezrukavnikov

## Directed Readings and Programs

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### Directed Reading Program MIT 2023-2024

- Read and made a presentation about  $h$ -cobordisms and Smale's theorem.  
Reference: Joye Chen
- Read and made a presentation about *Using the Borsuk-Ulam Theorem* by Jiří Matoušek.  
Reference: Elia Portnoy

### Preliminary Arizona Winter School MIT 2023-2024

- Watched recorded lectures and worked on problem sets with a TA for 9 weeks. The topics were elliptic curves with complex multiplication in 2023 and local fields in 2024.  
References: Ju-Lee Kim and Bjorn Poonen

### 18.099 Independent Study: Low-dimensional topology MIT 2024

- Read *Knots and Links* by Dale Rolfsen.  
Reference: Joshua Wang

### 18.099 Independent Study: The geometry of complex analysis MIT 2023

- Read *An Introduction to the Theory of Analytic Functions of One Complex Variable* by Lars Ahlfors.  
Reference: Joshua Wang

## Presentations

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Isomorphism between Hall algebra and shuffle algebra	MIT 2024
Happy sequences	MIT 2024
Sums of cubes	MIT 2024
The $h$ -cobordism theorem	MIT 2024
Heegard Splittings	MIT 2023
Applications of the Borsuk-Ulam Theorem	MIT 2023

## Volunteer Roles, Teaching, and Coaching

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### HMMT Problem Czar August 2022 – May 2023

- Wrote and chose problems for the February tournament and helped with the November tournament.

### Panamanian Mathematical Olympiad Member January 2021 – Present

- Wrote a handout and gave a lecture about Circle Geometry in a seminar for high school teachers.
- Organized the shortlist of proposed problems for the 2021 and 2022 Panamanian Mathematical Olympiad.  
Reference: Pedro Marrone

### Panamanian Training Program Instructor October 2020 – Present

- Served as Panama's Leader at the 2024 Iberoamerican Mathematical Olympiad.
- Served as Panama's Deputy Leader at the 2023 International Mathematical Olympiad.
- Currently serve as a math olympiad instructor, mainly in Geometry and Algebra.
- Gave the new students an introductory  $\text{\LaTeX}$  course.
- Served as Panama's Deputy Leader at the 2020 Iberoamerican Mathematical Olympiad.
- Served as a jury member at the 2020 Central American and Caribbean Mathematical Olympiad.  
Reference: Pedro Marrone

### AIPCV Math Olympiad Coach April 2018 – December 2020

- Trained the AIPCV school's team for the first and second rounds of the National Olympiad.
- Wrote a virtual book to train the team.

## Work Experience

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- MIT PRIMES Circle Mentor** MIT, 2023-2024
- Mentored high school students through the material of *The Knot Book* by Colin Adams in 2023 and *Thinking Geometrically: A Survey of Geometries* by Thomas Q. Sibley in 2024.  
Reference: Marisa Gaetz and Mary Stelow
- Undergraduate Assistant for 18.901 Introduction to Topology** MIT, 2023
- Graded homework, midterms, and the final exam. Wrote solutions and held office hours.
- Undergraduate Math Association Mentor** MIT, 2022
- Provided mentorship to students in introductory real analysis and algebra classes.
- Grader for 18.101 Analysis and Manifolds** MIT, 2023
- Graded homework.
- Grader for 18.100B Real Analysis** MIT, 2022
- Graded homework and wrote solutions.

## Selected Coursework

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### Algebra

- 18.725 Algebraic Geometry I
- 18.721 Introduction to Algebraic Geometry
- 18.705 Commutative Algebra
- 18.701 Algebra I and 18.702 Algebra II

### Topology

- 18.905 Algebraic Topology I and 18.906 Algebraic Topology II
- 18.904 Seminar in Topology
- 18.901 Introduction to Topology

### Number Theory

- 18.785 Number Theory I and 18.786 Number Theory II
- 18.783 Elliptic Curves
- 18.782 Introduction to Arithmetic Geometry

### Analysis

- 18.101 Analysis and Manifolds
- 18.100B Real Analysis

### Programming

- 6.100B Introduction to Computational Thinking and Data Science
- 6.100A Introduction to Computer Science and Programming in Python

### Physics

- 8.01 Physics I and 8.02 Physics II